# Bioinspired systems Hierarchy formation I: Collective motion and collective decision making



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Case study: Pedestrian motion; Models and their relations



- No clarified principles ("paradigm") yet
- Real-life problems, plenty of models
- Traffic models can be categorized according to the scale of the variables of the model:
  - Macroscopic,
  - Mesoscopic
  - Microscopic



Fredrik Johansson, Microscopic Modeling and Simulation of Pedestrian Traffic, Department of Science and Technology, Linköping University, 2013 2

# Macroscopic models / continuum dynamic approach

- Describes the macroscopic (or average) properties of the system
- Assumes that traffic can be regarded as a *fluid*, or continuum, disregarding the fact that it is composed of discrete entities such as cars or pedestrians
  - − No explicit reference to the underlying microscopic nature,  $\rightarrow$  no personal preferences
  - Central assumption:
    - no (sufficiently little) significant information is lost when the microscopic details are averaged out
    - the units are identical, unthinking elements
  - successful approach in physics
  - Bit less well founded in traffic modeling, but has been successful, primarily in car traffic modeling
- The basis of fluid dynamic models of pedestrian traffic is the two dimensional continuity equation

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \boldsymbol{q} = 0$$

where ho : mean density (  $ho=
ho({m r},t)$  ),

$$oldsymbol{q}=
ho u$$
 : mean flow (  $oldsymbol{q}=oldsymbol{q}(oldsymbol{r},t)$  ),

*u* : mean speed (the assumption that *u* is a function of the density, comes from observations) <sup>3</sup>

# Mesoscopic models

- Each individual is represented individually and can have individual properties (↔ Macroscopic)
- But the individual walker's behavior is still determined by average quantities

# Microscopic models

- describe every individual walker and its interaction with other walkers and the environment
- there is no averaging process → the heterogeneity of the population can be explicitly included (personal drives, motivations, preferred directions, etc.)
- Four basic types (partially overlapping, not well defined)
  - 1. cellular automaton based models
  - 2. agent based models
  - 3. game theoretic models
  - 4. force based models (Social force model)

# (1) Cellular automation based models

- Very first models (1980's), but still in use
- Discrete in space and time
- Each unit is a cell, either occupied by a pedestrian (or obstacle) or empty
- At each time step, pedestrians move into one of the neighboring cells or stay where they are.
- Limitation:
  - the size of a walker is fixed and constant over the population
  - Discrete size of movement at a time
    - (but different speeds and goals can be considered)
- Pro-s:
  - Computational efficiency
  - Simple update rules  $\rightarrow$  some general results are easy to obtain
  - The grids can be refined
  - One of the earliest models: Gipps and Marksjö (1985): (the "basics")
    - grid with quadratic cells
    - The preferred next cell is the one that reduces the remaining distance to the walker's destination the most
    - The navigation is modified by the presence of other walkers: repulsive potential around each walker





# (2) Agent based models

- basically CA models with "very complex" update rules
  - can be either continuous or discrete, both in space and time
  - can be governed by practically any type of behavioral rules.
  - often have a large set of behavioral rules, each dedicated to a specific situation.
  - The update procedure occurs in two steps:
    - 1. the agent determines the situation it is in by one or several test
    - 2. Executes the rule connected to that situation
  - Pro: can be very detailed
  - Con: high computational cost, hard to analytically provide properties

# (3) Game theoretic models

- Movement is an "action"
- Each pedestrian plans his/her path according to her beliefs about how other pedestrians will move in the future.
  - Example:
    - Pre defined strategies
    - an empirical distribution over the strategies of other players
    - Etc.

### (4) Force based models/social force models (SFM)

- Helbing and Molnár (1995)
- People walk in crowded environments by using automatic (subconscious) strategies for avoiding collisions and keeping comfortable distances
- These automatic strategies can be encoded as simple behavioral rules



Main idea: the influences of elements of the environment on the behavior of the pedestrians appear as social forces.

- Social forces are not "real" forces (in a Newtonian meaning), rather, are a description of the motivation of the pedestrian to change its velocity, induced by some elements in the environment.
- the effects of several social forces, just like regular forces, are assumed to add as vectors
- Operates in continuous space, allowing detailed representation of the geometry of the environment
- proven to reproduce several well known features of pedestrian traffic:
  - dynamic lane formation in opposing flows
  - oscillations at bottlenecks
  - evacuation scenarios

### Dynamic lane formation in opposing flows





#### **Experiment:**

Walkers self-organize into lanes to avoid interactions with oncoming pedestrians. This helps them to move faster than is otherwise possible. This happens effortlessly and requires no communication https://www.youtube.com/watch?v=J4J\_lOOV2E

#### Model:

F. Zanlungo, T. Ikeda and T. Kanda, Social force model with explicit collision prediction, Europhysics Letters, Volume 93, 68005

https://www.youtube.com/watch?v=u2kEM2Ed6Xk

#### An application for SFM: Panic in human crowd

According to the socio-psychological literature the characteristic features of escape panics:



- (1) People try to move considerably faster than normal
- (2) Individuals start pushing, and interactions become physical.
- (3) Moving and passing of a bottleneck becomes uncoordinated.
- (4) At exits arching and clogging are observed.
- (5) Jams build up
- (6) The physical interactions add up and cause dangerous pressures up to 4,450  $^{N}/_{m^{2}}$  which can bend steel barriers or push down brick walls

Dirk Helbing, Illés Farkas, and Tamás Vicsek: *Simulating dynamical features of escape panic*. Nature 407, 487-490 (2000)

### Model: Panic in human crowd

- Many-particle SPP system
- Main assumption: the individual behavior is influenced by a mixture of socio-psychological and physical forces

$$m_i \frac{\mathrm{d}\mathbf{v}_i}{\mathrm{d}t} = m_i \frac{\mathbf{v}_i^0(t)\mathbf{e}_i^0(t) - \mathbf{v}_i(t)}{\tau_i} + \sum_{j(\neq i)} \mathbf{f}_{ij} + \sum_W \mathbf{f}_{iW}$$

N: number of pedestrians (size of the crowd)  $m_i$ : mass of the *i*-th pedestrian

- $v_i^{0}$ : desired speed of individual *i*
- $e_i^{0}$ : preferred direction of individual i

 $\boldsymbol{v}_i(t)$ : actual velocity

 $au_i$ : characteristic ("reaction") time of individual i

 $f_{ij}$  and  $f_{iW}$ : "interaction forces": individual *i* tries to keep a velocity-dependent distance from other pedestrians *j* and walls *W*.



How crowd behaviour affects escape from a smoke-filled room. Previous simulations of pedestrian behaviour in crowds have used a model based on fluid flow through pipes, but these ignored the actions of individuals. According to the individual-centred model of Helbing *et al.*<sup>1</sup>, the evacuation of pedestrians from a smoke-filled room with two exits can lead to herding behaviour and clogging at one of the exits. By contrast, a traditional fluid-flow model would predict the efficient use of both exits. A more individual-centred approach is required to reproduce the behaviour of real crowds.

### Panic model – cont.

The psychological tendency of pedestrians i and j to avoid each other: repulsive interaction force:

$$A_i e^{\frac{r_{ij}-d_{ij}}{B_i}} \boldsymbol{n}_{ij}$$

If  $d_{ij} < r_{ij}$  then the pedestrians touch each other. In this case two additional forces (after granular interactions):

1. "Body force":

 $k(r_{ij}-d_{ij})\boldsymbol{n}_{ij}$ 

counteracting body compression

2. "Sliding friction force"

 $\kappa(r_{ij} - d_{ij})\Delta v_{ij}{}^{t} t_{ij}$ impeding relative tangential motion  $t_{ij}$  is the tangential direction, and  $\Delta v_{ij}{}^{t} = (v_j - v_i) \cdot t_{ij}$  is the tangential velocity difference

$$m_i \frac{\mathrm{d}\mathbf{v}_i}{\mathrm{d}t} = m_i \frac{v_i^0(t)\mathbf{e}_i^0(t) - \mathbf{v}_i(t)}{\tau_i} + \sum_{j(\neq i)} \mathbf{f}_{ij} + \sum_{W} \mathbf{f}_{iW}$$

N: number of pedestrians (size of the crowd)  $m_i$ : mass of the *i*-th pedestrian  $v_i^{0}$ : desired speed of individual *i*   $e_i^{0}$ : preferred direction of individual *i*   $v_i(t)$ : actual velocity  $\tau_i$ : characteristic ("reaction") time of individual *i*   $f_{ij}$  and  $f_{iW}$ : "interaction forces": individual *i* tries to keep a velocity-dependent distance from other pedestrians *j* and walls *W*.  $r_i(t)$  position of individual *i*  $A_i$  constant

B<sub>i</sub> constant

 $d_{ij} = \|\boldsymbol{r}_i - \boldsymbol{r}_j\|$  distance between the pedestrians' center of mass

 $oldsymbol{n}_{ij}$  : normalized vector pointing from pedestrian j to i

 $r_i$  : the radius of pedestrian i

 $r_{ij} = r_i + r_j$  the sum of the radii of pedestrians *i* and *j* 

 $\kappa$  : constant (large) k : constant (large)

g(x): zero, if the pedestrians do not touch each other  $(d_{ij} > r_{ij})$ , Otherwise equal to the argument x.

$$f_{ij} = \left\{ A_i e^{\frac{r_{ij} - d_{ij}}{B_i}} + k \cdot g(r_{ij} - d_{ij}) \right\} \boldsymbol{n}_{ij} + \kappa g(r_{ij} - d_{ij}) \Delta v_{ij}^{t} \boldsymbol{t}_{ij}$$

### Simulation results with reasonable parameters

#### Transition to incoordination due to clogging.

The outflow from a room is well coordinated and regular desired velocities are normal. But for desired velocities above 1.5 m/s(rush) an irregular succession of arch-like blockings of the exit and avalanche-like bunches of leaving pedestrians when the arches break appear.

2. "Faster-is-slower" effect due to impatience. Since clogging is connected with delays, trying to move faster can cause a smaller average speed of leaving (κ is large)

- fire



Simulation of 200 pedestrians evacuating a 15x15m room passing through a 1meter-wide door at a desired speed of 3.5m/s. https://www.youtube.com/watch?v=FidqTZiJvRA



### Simulation results with reasonable parameters

**3. Mass behavior.** Simulated situation: pedestrians are trying to leave a smoky room, but first have to find one of the invisible exits.

Each pedestrian *i* may either

- select an individual direction  $e_i$
- follow the average direction  $\langle e_j^0(t) \rangle_i$  of his neighbors j in a certain radius  $R_i$
- mix the two with a weight parameter  $p_i$

 $\mathbf{e}_i^0(t) = \operatorname{Norm}[(1 - p_i)\mathbf{e}_i + p_i \langle \mathbf{e}_j^0(t) \rangle_i]$ 

- − if  $p_i$  is small → individualistic behavior
- − if  $p_i$  is big → herding behavior
- $\rightarrow p_i$  is the "panic parameter" of individual i
- Best chances of survival: a certain mixture of individualistic and herding behavior





### Faster is slower in pedestrian evacuation



#### **Experiment (by GranularLab)**

Illustrative video experimentally demonstrating the Faster is Slower effect in pedestrian evacuation through narrow doors. The charts appearing in the vertical direction are spatio-temporal diagrams constructed by taking the lines of pixels displayed by green and stacking them vertically as time evolves. For more information: <u>http://journals.aps.org/pre/abstract/</u>...

https://www.youtube.com/watch?v=q-k4fCiiMlk

# Hierarchy formation and collective decision making



**a** Axon arborisation (the end part of a major kind of neuronal cell) shows a typical hierarchical tree-like structure in space.

**b** The wiring of a human brain. Hierarchy is not obvious, but closer inspection and additional MRI images indicate hierarchical functional operation.

c And this is a possible interpretation of how we think (thoughts being one of the end products of a functioning brain).

**d** The visualization (of the now commonplace) idea of the evolutionary tree.

*e* The famous first drawing of the branching of the phylogenetic tree with the "I think" note by Darwin.

*f* This complex tree with its hundreds of branches shows the birth of new variants (associated with new plant species) of a single protein!

**g** The well-known hierarchy of wolves, indicated by who is licking who (subordinates do this to those above them). The same behavior can be observed between a dog and her owner.

**h** Perhaps the only hierarchy named after a person. This pyramid is called "Maslov's hierarchy of needs".

*i* Visualization of the connections (call relations) between the various parts of a C+ software system (containing many thousands of entities and relations; the more closely related parts are color-coded and bundled).

*i* The strength of the directional correlations between pairs of pigeons in a flock (individuals being denoted by A0,...,A9). The asymmetric structure of the dominant part of the matrix (the entire matrix minus its symmetric components) indicates strictly hierarchical leader-follower relations.

**k** The picturesque representation of the two pyramids of medieval relations among the member s of a society: the left side corresponding to social organization, the right side corresponding to the religious organization.

I And finally: we show a huge community of relatively simple animals. Where is the hierarchy here? Nowhere: groups of many thousands of animals (large flocks of birds, schools of fish) typically do not display the signs of hierarchy (and, indeed, are assumed not to be hierarchically organized). 18

# Definition

- No compact, precise, widely accepted definition (diverse usage)
- Available definitions usually bypass the problem of clarification by using synonymous words
- Cambridge dictionary:
  - Hierarchy is "a system in which people or things are arranged according to their importance."
  - hierarchy corresponds to "the people in the upper levels of an organization who control it."
- Wikipedia: "A hierarchy (from the <u>Greek</u> hierarkhia, "rule of a high priest", from <u>hierarkhes</u>, "president of sacred rites") is an arrangement of items (objects, names, values, categories, etc.) in which the items are represented as being "above", "below", or "at the same level as" one another."

# **Definition: hierarchy**

We talk about *hierarchy* in situations in which the *entities of a system can be classified into levels in a way that elements of a higher level determine or constrain the behavior and/or characteristics of entities in a lower level.* That is, at the heart of hierarchy, we find control of behavior.



**Definition**: A system is *hierarchical* if it has elements (or subsystems) that are in dominantsubordinate relation to each other. A unit is *dominant* over another unit to the extent of its ability to influence the behavior of the other. In this relationship, the latter unit is called *subordinate*.

### Comments on the definition of hierarchy - I

- It does not tell us how hierarchical the entire *system* is.
- It tells whether the *elements* (or subsystems) are in hierarchical relation or not? (manifesting itself in a dominant-subordinate relationship)
- It also tells the *origin* (reason) and *extent* of the dominant-subordinate relationship
- Rock–paper–scissors game:
  - The rock blunts the scissors (and hence "disarms" it, beats it)
  - The scissors cut the paper, and
  - The paper covers the rock.
- From a graph-theoretical point of view: where to put the arrows and what they mean there.
- It does not tell us how hierarchical the entire system is.
- "Measuring the level of hierarchy" in directed graphs has an entire literature



**Definition**: A system is *hierarchical* if it has elements (or subsystems) that are in dominant-subordinate relation to each other. A unit is *dominant* over another unit to the extent of its ability to influence the 21 behavior of the other. In this relationship, the latter unit is called *subordinate*.

#### Comments on the definition of hierarchy - II

- This definition implies that the units *behave* somehow, or have some observable characteristics. → entities without observable behavior or characteristics cannot form hierarchical structure.
- Hierarchy might vary over time.
  - As certain characteristics of the group members change (for example, the physical strength of the individuals in a pack of wolves), so do their ranks.
- During different group activities, the influence of the members might vary.
  - $\rightarrow$  hierarchy is context/task-sensitive, even within the same group!
  - E.g.: pigeon flocks: Feed / collective flights.
  - even more starkly expressed in human groups
- The influence can either be
  - *forced* by the higher-ranked individual (e.g., when a higher-ranked animal does not let a lower-ranked one near the food source), or it can be
  - voluntary (for example, leader-follower relationships during flight).
- A higher-ranked unit, by influencing the behavior of other units more extensively, has a larger effect on the collective (emergent) group behavior as well.

Name	Description	example
Order hierarchy	Basically an ordered set, in which a value is assigned to each element characterizing one of its arbitrarily chosen features, which defines its rank. The network behind the system is neglected or it does not exist.	<ul> <li>ranking of artists, e.g., painters or sculptors, based on the average price of their artworks</li> <li>firms ordered by their <ul> <li>number of employees</li> <li>annual income, etc.</li> </ul> </li> </ul>



Name	Description
Nested Embedded Containment Inclusive Hierarchy	A structure in which entities are embedded into each other. Higher level entities consist of and contain lower level entities. Close relation to community detection in graphs
A subsumptive containment hierarchy (a.k.a. taxonomic hierarchy)	A structure in which items are classified from specific to general



A structure in which

embedded into each

**Higher level entities** 

lower level entities.

Close relation to

in graphs

consist of and contain

community detection

#### Description

other.

entities are

Nested Embedded Containment Inclusive Hierarchy

Name

#### A *Compositional* containment hierarchy (a.k.a. *level*

hierarchy)

Describes how a system is composed of subsystems, which are also composed of subsystems, etc.

• "Hierarchy of life"



Name	Description	example
Flow (or control) hierarchy	<ul> <li>"Intuitively," this is an acyclic, directed graph.</li> <li>Nodes are layered into</li> <li>levels: nodes on higher</li> <li>levels: nodes on higher</li> <li>levels influence nodes on</li> <li>lower levels, and the</li> <li>influence is represented by</li> <li>edges.</li> <li>Layers refer to power, that is,</li> <li>an entity on a higher level</li> <li>gives orders or passes on</li> <li>information to entities on</li> <li>lower levels.</li> <li>("flow of order")</li> <li>How certain entities control</li> <li>other entities.</li> </ul>	<ul> <li>Armies, churches, schools, political parties, institutions, etc.</li> <li>Downwards: orders flow along the edges;</li> <li>Upwards: requests or information.</li> </ul>

- These types are not independent of each other
- many systems can be described by more than one type (e.g. army: flow & compositional containment)
- Both order and nested hierarchies can be converted into a flow hierarchy.

# Describing hierarchical structures

- Most commonly used mathematical tool: *graphs*
- Primarily they are connected to systems embodying *flow hierarchy* 
  - observations, experiments, computer simulations are likely to return flow hierarchy;
  - all other hierarchy types can be transformed into flow hierarchy in a rather straightforward way
- We can measure the hierarchical level of the *graph* (not the system itself)
- No "most appropriate" measure (many structure is "matter of intuition / taste")
- Most of the proposed measures take values on the [0, 1] interval

Some common approaches For directed and undirected graphs

- Fraction of edges participating in cycles
- Minimum fraction of edges to be removed to make the graph cycle-free



# Random Walk Measure

#### • Motivation:

- it is not correct to treat all directed acyclic graphs as already being maximally hierarchical, independent of their inner structure.
- common intuition: a hierarchical structure often corresponds to a multi-level pyramid in which the levels become more and more wide as one descends from the higher levels towards the lower ones
- Assumption: there is information/instruction flow from the high-ranking nodes towards the bottom ones
- Method:
  - find the sources by dropping down random walkers onto the nodes who then move *backwards* along the links
  - Once a steady state is reached, the *density* of such random walkers is interpreted as being proportional to the *rank* of the node:
    - high random walker density: the vertex is a *source* of information (high rank)
    - low density: the vertex is just a "receiver" of orders (low rank)
  - The hierarchical nature of the network: estimated based on the *distribution* of random walker densities
    - Homogeneous: the source of information/order cannot be pinpointed: not hierarchical
    - Inhomogeneous: clear information sources: the network is hierarchical.

Czégel D, Palla G (2015) Random walk hierarchy measure: what is more hierarchical, a chain, a tree or a star? Sci Rep 5:17994

## Global Reaching Centrality ("GRC")

- Central idea: to give a rank to each node by measuring its "impact" on other nodes
  - "Impact": the ratio of vertices that can be reached from the focal node *i* – this is the "local reaching centrality"
  - In a directed, un-weighted graph  $C_R(i)$  is the number of vertices that can be reached from node *i*, divided by N-1
  - The level of hierarchy is inferred from the *distribution* of the  $C_R(i)$  values
    - Heterogeneous distribution: hierarchical network
    - Homogeneous distribution: non-hierarchical graph
- From distribution to number:
  - Let  $C_R^{max}$  denote the highest  $C_R(i)$  value in a graph G=(V,E)
  - Then *GRC*, the Global Reaching Centrality is:

$$\operatorname{GRC} = \frac{\sum_{i \in V} \left[ C_R^{\max} - C_R(i) \right]}{N - 1}$$

### Global Reaching centrality ("GRC")

Example: GRC distribution for three different network types:

- Erdős-Rényi (random) (not hier)
- Scale-free (moderately hier)
- Tree (highly hier)

$$\operatorname{GRC} = \frac{\sum_{i \in V} \left[ C_R^{\max} - C_R(i) \right]}{N-1} \quad 0.000$$

Network type	GRC
Erdős-Rényi	0.058 ± 0.005
Scale-free	$0.127 \pm 0.008$
Tree	$0.997 \pm 0.001$



2000, of the appropriate graph type.

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Observations and measurements

# **Dominance hierarchy**

- Solitary vs. social lifestyles
- If the ratio of advantages/disadvantages is higher, then the given animals will knit into groups
- A mechanism is needed to reduce the level of aggression triggered by the competition
- Regulate access to resources.
- The mechanism is simple: higher ranked individuals have primacy compared to their lower level mates.
- As one advances in the evolutionary tree, the structure of the dominance hierarchy gets more and more pronounced and complex, accompanied by more and more sophisticated strategies by which individuals try to get higher and higher ranks.
- Chimpanzees (few decades ago believed to be solely human):
  - coalition formation
  - manipulation
  - exchange of social favors
  - adaptation of rational strategies
- Obvious advantage: less fight











# Leadership in motion The relation of collective motion to collective decision making

- If the group is to stay together, individuals constantly have to make decisions regarding
  - When and where to forage, to rest
  - How to defend themselves from predators
  - How to navigate towards a distant targets
  - Etc.
- **Cost/benefit ratio** (from the viewpoint of the members)
  - Preferred outcome usually differs (information, experience, inner state, etc.)
  - "consensus cost": cost paid by the animal who foregoes its preferred behavior in order to defer to the common decision

### First studies – two basic types

#### Despotic system

- One or a few individual decides
- This can increase the efficiency

Egalitarian / democratic

- Members contribute to the outcome about the same degree
- Smaller average consensus cost
- In nature, both types have been observed
- Sometimes mixed (alternating according to the circumstances)
  - Pairs of pigeons, GPS (2006)
    - Small conflict over the preferred direction: consensus (average)
    - Above a certain threshold: one of them becomes the leader or they split up
  - Similar observations: Wild baboons, GPS (2015)
    - They follow the majority of the "initiators" (those starting off in a certain direction). (And not the dominant individuals)
    - If two groups of initiators (with similar size) heading in different directions:
      - If the angle is less than ~90°  $\rightarrow$  the animals compromise
      - Big angle: they choose one direction over the other (randomly)

### Models for leadership

- Extension of the "Couzin model"
- No individual recognition, no signaling mechanism
- Non-informed individuals: are not required to know how many and which individuals has information
- Vice versa: Informed individuals are not required to know anything about the information-level of their mates and that how the quality of their information was compared to that of others.

#### The model:

• Rule 1: highest priority

 Individuals attempt to maintain a certain distance among themselves by turning away from those neighbors *j* which are within a certain distance towards the opposite direction:

$$\vec{d}_i(t + \Delta t) = -\sum_{j \neq i} \frac{\vec{r}_j(t) - \vec{r}_i(t)}{\left| \vec{r}_j(t) - \vec{r}_i(t) \right|}$$

#### Simulating Swarm Intelligence

Reseachers created a model of swarm behavior by programming individuals to maintain personal space while turning and moving in the same direction as others.

# 

Sources: Iain D. Couzin; Journal of Theoretical Biology

#### Area of repulsion

A simulated animal (~\_) tries to maintain a spherical area of personal space by avoiding collision with other animals entering the area.

#### Area of orientation

The simulated animal will try to orient itself and move in the same direction as other animals in this region.

#### Area of attraction

The animal will try to move toward other animals in this region, encouraging group formation and cohesion.

 $\vec{d}_i$ : desired direction of individual i $\vec{r}_i$ : position of particle i $\vec{v}_i$ : direction of unit i

[Couzin, I.D., Krause, J., Franks, N.R., Levin, S.A., 2005. Effective leadership and decision-making in animal groups on the move. Nature 433, 513–516.]

# Models for leadership

#### The model (cont):

#### • Rule 2

If there are no mates within the range of repulsion, than the individual will attempt to align with those neighbors *j*, which are within the range of alignment:

 $\rightarrow$  The desired direction:

$$\vec{d}_i(t + \Delta t) = -\sum_{j \neq i} \frac{\vec{r}_j(t) - \vec{r}_i(t)}{\left|\vec{r}_j(t) - \vec{r}_i(t)\right|} + \sum_{j \neq i} \frac{\vec{v}_j(t)}{\left|\vec{v}_j(t)\right|}$$

 $\vec{d}_i$ : desired direction of individual i $\vec{r}_i$ : position of particle i $\vec{v}_i$ : direction of unit i

- Corresponding unit vector:  $\hat{d}_i(t) = \vec{d}_i(t) / |\vec{d}_i(t)|$
- Introducing "influence": a portion of the group (p) is given information/motivation about a preferred direction, described by the (unit) vector  $\vec{g}$ .
- The rest of the group does not have directional preference.

Informed individuals balance their

- social alignment  $\hat{d}_i(t)$  (the unit vector of  $\vec{d}_i(t + \Delta t) = -\sum_{j \neq i} \frac{\vec{r}_j(t) \vec{r}_i(t)}{|\vec{r}_i(t) \vec{r}_i(t)|} + \sum_{j \neq i} \frac{\vec{v}_j(t)}{|\vec{v}_i(t)|}$ ) and
- preferred direction  $\vec{g}_i$

with the weighting factor  $\boldsymbol{\omega}$ :

$$\vec{d}_i(t + \Delta t) = \frac{\hat{d}_i(t + \Delta t) + \omega \vec{g}_i}{\left|\hat{d}_i(t + \Delta t) + \omega \vec{g}_i\right|}$$

- $\omega$  can exceed 1: the individual is influenced more by its own preferences than by its mates
- "Accuracy" of the group: normalized angular deviation of the group direction around the preferred direction  $\vec{g}_i$

#### **Results:**

 for fixed group size, the accuracy increases asymptotically as the portion p of the informed members increases

(...that is...)

 the larger the group, the smaller the portion of informed members is needed, in order to guide the group towards a preferred direction



# **Conflicting preferences**

#### Informed individuals might differ in their preferred direction

- 1. If the number of individuals preferring one or another direction is equal: the group direction depends on the degree to which the preferred directions differ
  - If it is small: the group will go in the average preferred direction of all informed individuals
  - If it is big: individuals select randomly one or another preferred direction
- 2. If the number of informed individuals preferring a given direction increases
  - the entire group will go into the direction preferred by the majority (even if that majority is small)

Collective group direction when two groups of informed individuals differ in their preferences - model results



- Vertical axis: the degree of the most probable group motion.
- The first group (consisting of  $n_1$  informed individuals) prefers the direction characterized by 0 degrees (dashed line),
- The second group (consisting of  $n_2$  informed individuals) prefers a direction between 0 and 180 degrees (horizontal axis)
- Solid white lines are for reference only, representing the direction of the average vector of all informed individuals
- The group consists of 100 individuals altogether

Source: Couzin, I.D., Krause, J., Franks, N.R., Levin, S.A., 2005. Effective leadership and decision-making in animal groups on the move. Nature 433, 513–516.

# The role of uninformed individuals – simulations vs. experiments

- Question: under what conditions can a selfinterested and strongly opinionated minority exert its influence on group movement decisions?
- Simulations:
  - Based on the "Couzin model"

$$\vec{d}_i(t + \Delta t) = \frac{\hat{d}_i(t + \Delta t) + \omega \vec{g}_i}{\left|\hat{d}_i(t + \Delta t) + \omega \vec{g}_i\right|}$$

- If all individuals are biased:
  - If the strength of the majority preference  $(\omega_1)$  is equal to or stronger than the minority preference  $(\omega_2)$ , the group has a high probability of reaching the majority-preferred target.
  - Increasing  $\omega_2$  (beyond  $\omega_1$ ) can result in the minority gaining control
- If there are uninformed individuals ( $\omega_3 \approx 0$ ):
  - (most animal groups are like this)
  - Adding uninformed individuals tends to return control spontaneously to the numerical majority
  - this effect reaches a maximum and then begins to slowly diminish, and eventually, noise will dominate



A sharp transition from a minority- to majoritycontrolled outcome in the model as the density of uninformed individuals is increased.

 $(\omega_{minority} > \omega_{majority})$ 

# Experiment

- golden shiners
- two groups of initiators (with sizes  $N_1$  and  $N_2$ ) with different preferred directions (blue and yellow target)
- some did not have direction preference
- $N_1 > N_2$  ( $N_1 = 6$  and  $N_2 = 5$ )
- Among the trained fish,  $\omega_{yellow}$  is "by nature" >  $\omega_{blue}$
- Simulations predict a large effect for a relatively small number of naïve individuals;  $N_3 = 0, 5, 10$ .
- When all individuals exhibit a preference  $(N_3 = 0)$ then the minority  $N_2$  dictates the consensus (even though the fish trained to the blue target are more numerous).
- When untrained individuals are present, they increasingly return control to the numerical majority N<sub>1</sub>.
- If individuals with the stronger preference were also in the numerical majority: the majority was more likely to win (72% of trials overall), and the presence of uninformed individuals had no effect





Experimental set-up

Couzin et al, 2011, Uninformed individuals promote democratic consensus in animal groups. Science, 334(6062):1578-80

#### Lessons

- Leadership might emerge from the differences of the level of information possessed by the group members
- information can be pertinent
   → leadership can be transient
   and transferable too