Opinion dynamics

Bioinspired Systems – 2023 Nov 13

Technical information

The presentations (pdf versions of the ppt files) are available on https://hal.elte.hu/~lanna/



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Questions from last class

1) The pigeons were both females and males. The sexual dimorphism is very small in their case (even experts have a hard time to determine their sex), and it does not play a role in their hierarchy.

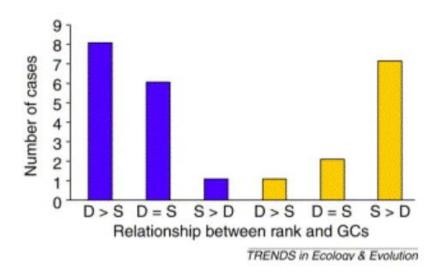


Fig. 2. The relationship between basal glucocorticoid (GC) levels and social status in species with cooperative breeding (purple bars) and in other social systems (yellow bars). D and S represent dominant and subordinate: D > S means that GC levels were significantly higher in dominant individuals, D=S means that GC levels are not detectably affected by rank, and S>D means that GC levels were significantly higher in subordinates.

				Reproductive		Method
		Basal		suppression		of
		GC	Social	of	Captive or	sampling
Species	Sex	pattern	system	subordinates ^c	wild study	GCs
Primates						
Squirrel	M	Sub	Social	No	Captive	Blood
monkey		>Dom				
Saimiri	M	Dom	Social	No	Captive	Blood
sciureus		>Sub				
Rhesus	M	Dom	Social	No or low	Captive	Blood
macaque	***	=Sub	boerar	skew	(enclosure)	
Масаса		545		J.C.	(enclosure)	
mulatta						
Lesser	M	Dom	Solitary	Low skew	Captive	Blood
mouse	IVI	=Sub	Somary	LOW SKEW	Сариче	blood
lemur		-3 u b				
Microcebus						
murinus						
	N	Cb	Carial	I ann alama	147:1 J	Disad
Olive	M	Sub	Social	Low skew	Wild	Blood
baboon		>Dom				
Papio anubis						

Scott Creel, **Social dominance and stress hormones**, *Trends in Ecology & Evolution*, Volume 16, Issue 9, 2001

Part 1 - Opinion dynamics



Opinion dynamics

- The scientific field aiming to understand the way "opinions" spread in human communities.
 - The community is usually described by means of networks
 - Nodes are individuals
 - Links are the ties (connections)
 - Direction
 - Strength
 - "opinion" (or "state" of the node) is usually described by a scalar (binary or continuous)
- Close relation to fields studying other spreading phenomena
 - Infection spreading



- Relevant general questions include:
 - What are the fundamental interaction mechanisms ("local rules")
 that allow for the emergence of
 - Consensus / polarization / fragmentation
 - a shared culture
 - a common language, etc. ...
 - What favors the homogenization process? What hinders it?

- Simplification arises from the fact that opinion formation is a complex process affected by the interplay of a vast amount of different elements, including the
 - Individual predisposition / family background ("identity")
 - Background knowledge
 - External information (e.g. public media)
 - Etc.

Typical ("classical") models

- Consider a finite number of connected agents
- each possessing opinions, described by variables,
- Assume certain *local rules* by which opinions change
 - Change of opinions result from interactions, either with peers or other sources.

Opinions:

- Variables:
 - one dimensional/multidimensional vector
 - discrete (the components can assume a finite number of states)
 - or continuous (values in the domain of real numbers)

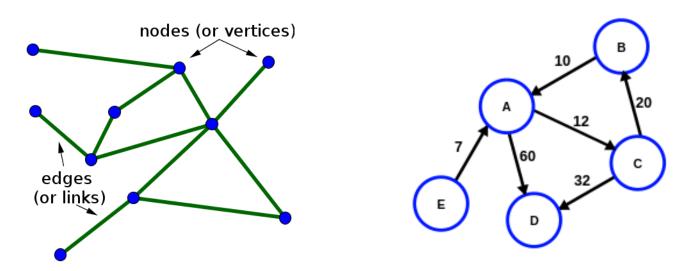
Connections:

- Topology of the interaction NW (what is realistic?)
- "Heritage" from physics: lattices or all-to-all (MF);
 (hardly realistic in social context)

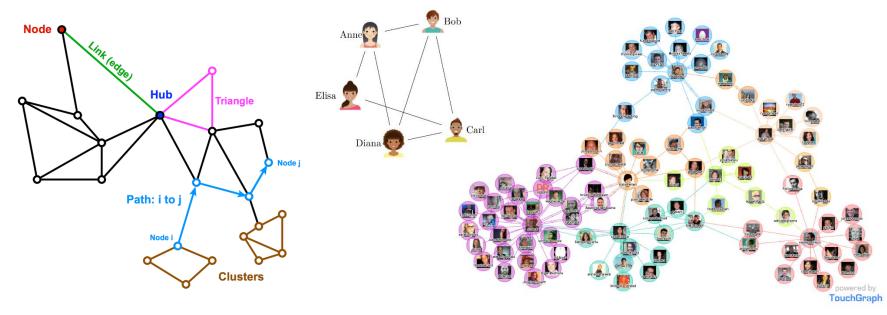
- Drawbacks of the models:
 - many simplifications;
 - many of the omitted parameters (most probably) have a fundamental effect in the final dynamics
 - Hard to say when are the results "good" (polarization)

- (It is said to have) success in:
 - Agreement
 - Cluster formation
 - Transition between order (consensus) and disorder (fragmentation)

Basic concepts of networks



With some network analysis



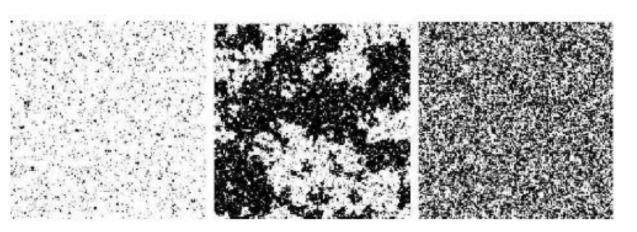
Binary opinions

- Discrete, one dimensional
- 0/1; yes/no; etc
- Interpretation in op. dyn: political questions infection models: infected / not market behavior: selling/buying

Very first opinion dynamic model by physicist: 1971, Weidlich

Ising model metaphor

- Consider a collection of N spins (agents): s_i
- They can assume two values: +/- 1
- Each spin is energetically pushed to be aligned with its nearest neighbors.
- The total energy is: (the sum runs on the pairs of nearest-neighbors) $H=-\frac{1}{2}\sum_{\langle i,j\rangle}s_is_j$
- Elementary move:
- a single spin flip is accepted with probability $\exp(-\Delta E/k_BT)$
 - ΔE : change in the energy
 - T: temperature (In ferromagnetic systems thermal noise injects fluctuations tends to destroy order)
 - Critical temperature T_c : above: the system is macroscopically disordered under: long-range order is established



Snapshots of equilibrium configurations of the Ising model (from left to right) below, at and above T_c .

Relation to opinion dynamics models

- Each agent has one opinion represented as a spin:
 a choice between two options
- Spin couplings: peer interactions (social conformity)
- Magnetic field: external information / propaganda
- Simple, but attractive model

Potts model (1951)

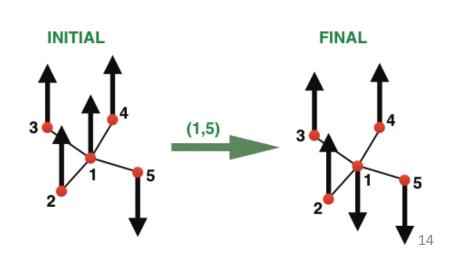
- a generalization of the Ising model
- Each spin can assume one out of q values
- equal nearest neighbor values are energetically favored.
- The Ising model corresponds to the special case $q=2^{13}$

Voter model

- Originally introduced to analyze competition among species, early 1970s
- Rather crude description of any real process
- Popular: it is one of the very few non-equilibrium stochastic processes that can be solved exactly in any dimension
- its name stems from its application to electoral competitions
- The model:
 - each agent in a population of N holds one of two discrete opinions: s = +/-1
 - agents are connected by an underlying graph (topology)
 - At each time step:

a random agent i is selected (1) along with one of its neighbors j (5) and the agent takes the opinion of the neighbor: $s_i = s_i$

(alignment *not* to the majority, but to a random neighbor)

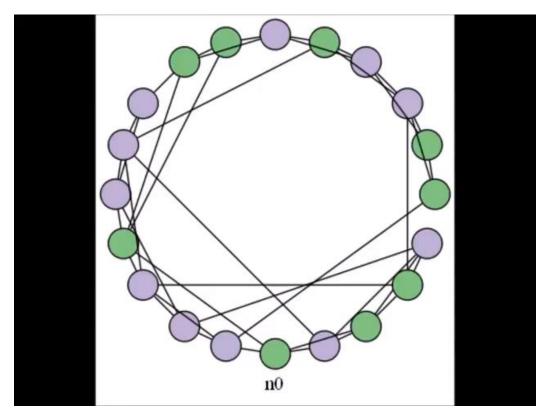


Behavior of the Voter model

- Has been extensively studied
- If people are modeled as vertices in a *d*-dimensional hyper-cubic lattice.
 - − For finite system: for any dimension d of the lattice, the voter dynamics always leads to one of the two possible consensus states: each agent with the same opinion s = 1 or s = -1.
 - The probability of reaching one or the other state depends on the initial state of the population.
 - Time needed for reaching the consensus state:
 - $d = 1: T_N \sim N^2$
 - $d = 2: T_N \sim N \ln N$
 - $d > 2: T_N \sim N$
 - For infinite systems: consensus is reached only if d ≤ 2

Extensions of the voter model

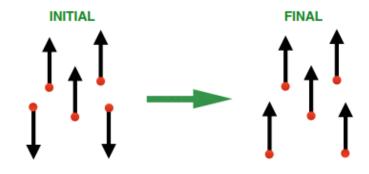
- Introduction of "zealots": individuals who do not change their opinion
- Constrained voter model:
 - agents can be leftist, rightist, centralist;
 - Extremists do not talk to each other (discrete analogue of the bounded confidence model)
- Communication is based on various NW



Voter model on a small world network https://www.youtube.com/watch?v=VmhSTdrsimk

Majority rule model

- Motivation: describing public debates
- (Galam, 2002)
- **Definition:**
 - Population of N agents
 - A fraction p_{+} of agents has opinion +1
 - $p_{\perp} = 1 p_{\perp}$ has opinion -1
 - Everybody can communicate with everybody else
 - At each interaction:
 - A group of r agents are selected at random ("discussion group")
 - Consequence of this interaction: each agents take the majority opinion inside the group
 - r is taken from a given distribution at each step
 - If r is odd: there is always a clear majority
 - If r is even: in case of tie: a bias is introduced in favor of one of the options (Inspired by the principle of "Social inertia" holding that people are reluctant to accept a reform if there is no clear majority in its favor)



Basic features of the MR model

- Original definition:
 - There is a *threshold fraction* p_c such that if $p_0^+ > p_c$, then all agents will have opinion +1 in the long run
 - Time needed for the consensus: $T_N \sim \log N$
 - If the group sizes r are odd: $p_c(r) = 1/2$ (due to the symmetry)
 - If they can be even too: $p_c < 1/2$, that is, the favored opinion will eventually win, even if it was originally in minority
- For fixed odd r, group size & mean field approach: analytically solvable for both finite N and for $N \rightarrow \infty$

Many variants and modifications

Social impact theory

- Bibb Latané (psychologist), 1981:
- social impact: any influence on individual feelings, thoughts or behavior that is created from the real, implied or imagined presence or actions of others.

("Collective" behavior)

- The impact of a social group on a subject depends on:
 - The number of individuals within the group
 - Their convicting power
 - Their distance from the subject (in an abstract space of personal relationships)
- Originally a cellular automata was introduced by Latané (1981) and later refined by Nowak et al (1990).

Social impact theory – the model

- A population of N individuals
- Each individual i is characterized by
 - an opinion $\sigma_i = \pm 1$
 - Persuasiveness p_i : the capability to convince someone to change opinion (a real value)
 - Supportiveness: s_i: the capability to convince someone to keep its opinion (a real value)
 (these are assumed to be random)
- The distance between agents i and j d_{ij}
- α >2 parameter defining the how fast the impact decreases with the distance

$$I_i = \left[\sum_{j=1}^N \frac{p_j}{d_{ij}^{\alpha}} (1 - \sigma_i \sigma_j)\right] - \left[\sum_{j=1}^N \frac{s_j}{d_{ij}^{\alpha}} (1 + \sigma_i \sigma_j)\right]$$

Persuasive impact (to change)

supportive impact (to keep opinion)

$$\sigma_i(t+1) = -sgn[\sigma_i(t)I_i(t) + h_i]$$

h_i: personal preference, originating from other sources (e.g. mass media)

a spin flips if the pressure in favor of the opinion change overcomes the pressure to keep the current opinion ($I_i > 0$ for vanishing h_i)

General behavior of the social impact model

- In the absence of individual fields (personal preferences):
 - the dynamics leads to the dominance of one opinion over the other, but not to complete consensus.
- In the presence of individual fields:
 - these minority domains become metastable: they remain stationary for a very long time, then they suddenly shrink to smaller clusters, which again persist for a very long time, before shrinking again, and so on ("staircase dynamics").

- Many modification / extensions:
 - Learning
 - Presence of a strong leader
 - Etc.

Schweitzer and Holyst included: (2000)

- Memory: reflecting past experience
- A finite velocity for the exchange of information between agents
- A physical space, where agents move.

Continuous opinions

- In many cases more realistic
- Requires different framework
 - Concepts like "majority" or "opinion equality" don't work
 - Has a different 'history'
- First studies (end of 1970's and 80's):
 - Aimed to study the conditions under which a panel of experts would reach a common decision ("consensus")
 - By applied mathematicians
- Typically:
 - Initial state: population of N agents with randomly assigned opinions, represented by real values within some interval.
 discrete op. dyn. ← all agents start with different opinions
 - Possible scenarios: more complex
 - Opinion clusters emerging in the final stationary state:
 - one cluster: consensus,
 - two clusters: polarization
 - more clusters: fragmentation

Bounded confidence (BC) models

- In principle: each agent can interact with every other
- In practice: (often) there is a real discussion only if the opinions are sufficiently close:

bounded confidence

- In the literature: introducing a real number ε: "uncertainty" or "tolerance", such that:
- An agent with opinion x, only interacts with those whose opinion lies in the interval $]x-\epsilon$, $x+\epsilon[$
- ("Homophily")

Deffuant model

- population of N agents
- nodes of a graph: agents may discuss with each other if they are connected.
- Initially: each agent i is given an opinion x_i randomly chosen from the interval [0, 1].

Dynamics:

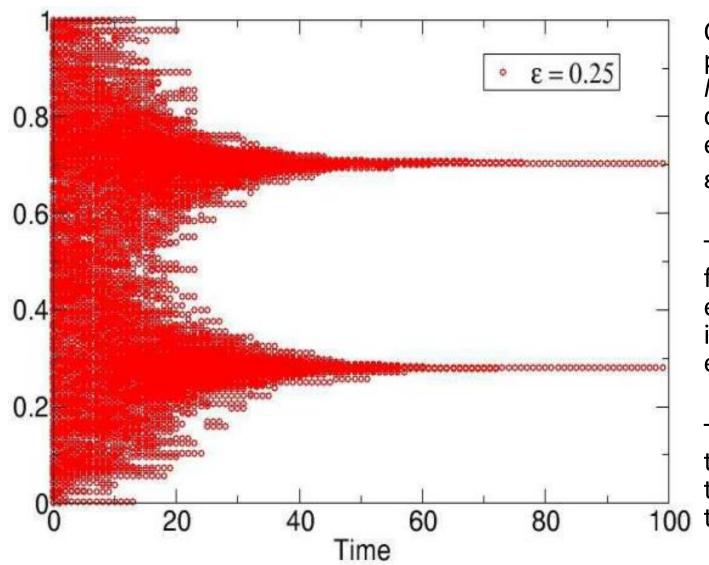
- random binary encounters, i.e., at each time step, a randomly selected agent discusses with one of its neighbors, also chosen at random.
- Let i and j be the pair of interacting agents at time t, with opinions $x_i(t)$ and $x_i(t)$
 - if the difference of the opinions $x_i(t)$ and $x_j(t)$ exceeds the threshold ε , nothing happens
 - If $|x_i(t) x_i(t)| < \varepsilon$, then

$$x_i(t+1) = x_i(t) + \mu[x_j(t) - x_i(t)]$$
$$x_j(t+1) = x_j(t) + \mu[x_i(t) - x_j(t)]$$

Behavior of the Deffuant model

- For any value of ϵ and μ , the average opinion of the agents' pair is the same before and after the interaction \rightarrow the global average opinion (1/2) of the population is invariant
- Patches appear with increasing density of agents
- Once each cluster is sufficiently far from the others (the difference of opinions in distinct clusters exceeds the threshold):
 - only agents inside the same cluster interact
 - the dynamics leads to the convergence of the opinions of all agents in the cluster
- In general:
 - the *number and size of the clusters* depend on the threshold ϵ (if ϵ is small, more clusters emerge)
 - the parameter μ affects the convergence time
 - (when μ is small, the final cluster configuration also depends on μ)

Behavior of the Deffuant model

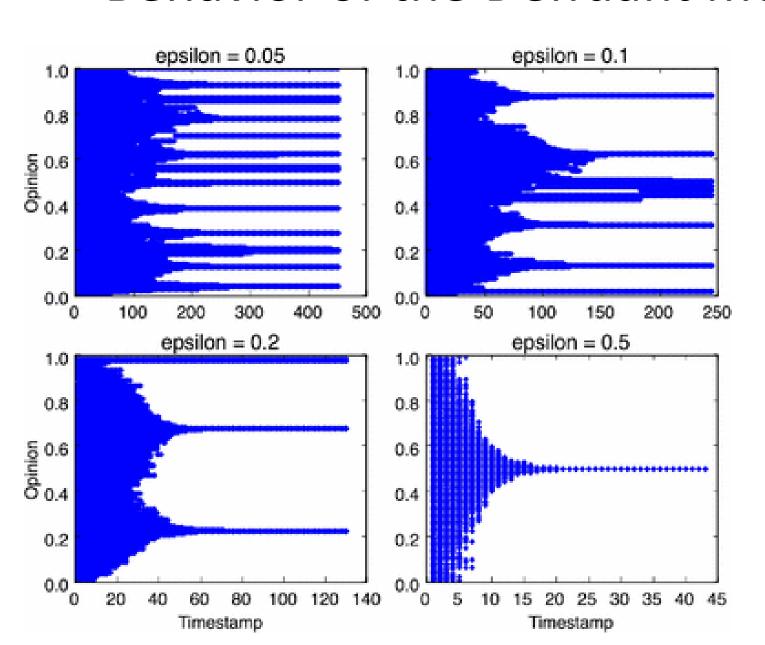


Opinion profile of a population of N=500 agents during its time evolution, $\epsilon = 0.25$.

The population is fully mixed, i.e., everyone may interact with everybody else.

The dynamics leads to a polarization of the population in two factions.

Behavior of the Deffuant model



Hegselmann-Krause (HK) model

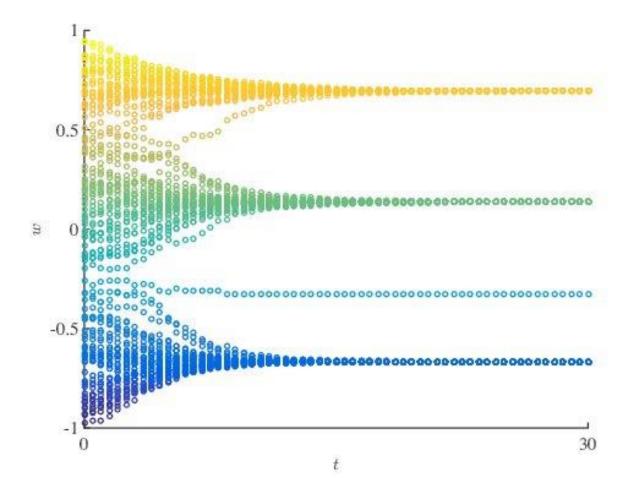
- Hegselmann and Krause, 2002
- Similarities with the Deffuant model:
 - Opinions take real values in an interval, say [0, 1]
 - An agent i (with opinion x_i), interacts with neighboring agents whose opinions lie in the range $[x_i-\varepsilon, x_i+\varepsilon]$
- Difference: update rule
 - An agent i does not interact with one of its compatible neighbors (like in Deffuant), but with all its compatible neighbors at once.
 - intended to describe formal meetings

$$x_i(t+1) = \frac{\sum_{j:|x_i(t) - x_j(t)| < \epsilon} a_{ij} x_j(t)}{\sum_{j:|x_i(t) - x_j(t)| < \epsilon} a_{ij}}$$

- a_{ii} : elements of an adjacency matrix describing the communication network.
- Agent i takes the average opinion of its compatible neighbors.

Behavior of the Hegselmann-Krause model

- fully determined by the uncertainty ε
- Need lot of computation power (due to the average calculation)



The dynamics develops similarly to the Deffuant model:

- Leads to the same pattern of stationary states, with the number of final opinion clusters decreasing if ε increases.
- for $\varepsilon > \varepsilon_c$ (a threshold) there can be only one cluster

Cultural dynamics

Multidimensional vector model

Mostly: opinion: scalar variable

",culture": a vector of variables

The typical questions are similar:

- what are the microscopic mechanisms that drive the formation of cultural domains?
- What is the ultimate fate of diversity?
- Is it bound to persist or all differences eventually disappear in the long run?
- What is the role of the social network structure?

Axelrod model

- Axelrod, 1997
 - Attracted lot of interest both from social scientists and physicists
 - Reason (soc. sci): inclusion of two fundamental mechanisms:
 - Social influence: the tendency of individuals to become more similar when they interact
 - Homophily: the tendency of alikes to attract each other, so that they interact
 more frequently
 - These two ingredients were generally expected to generate a selfreinforcing dynamics leading to a global convergence to a single culture.
 - But it turns out that the model predicts in some cases the persistence of diversity. (The importance of minimal models!)
 - From the viewpoint of stat. phys:
 - is a "vectorial" generalization of opinion dynamics models
 - gives rise to a very rich and nontrivial phenomenology, with some genuinely novel behavior

Axelrod's model

Individuals:

- are nodes on a network (or on the sites of a regular lattice original version)
- They are endowed with F integer variables $(\sigma_1, \ldots, \sigma_F)$ (describing their "culture")

The variables are the "cultural features"

- Each σ_i (feature) can assume q values: $\sigma_f = 0,1,...,q-1$
 - q: number of possible traits (modeling the different "beliefs, attitudes and behavior" of individuals

An elementary step:

- an individual i and one of its neighbors j are selected
- The overlap between them is computed:

$$\omega_{i,j} = \frac{1}{F} \sum_{f=1}^{F} \delta_{\sigma_f(i),\sigma_f(j)}$$

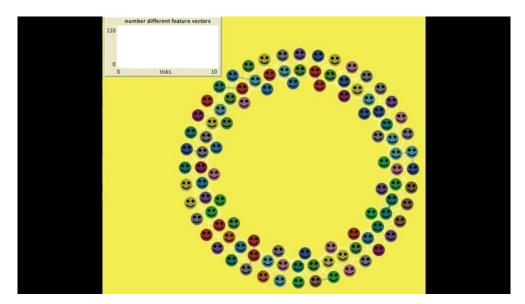
Where $\delta_{i,i}$ is the Kronecker delta

- $-\omega_{i,i}$: probability of interaction between i and j
 - If they interact: one of the features for which traits are different $(\sigma_f(i) \neq \sigma_f(j))$ is selected and the trait of the neighbor is set equal to $\sigma_f(i)$
 - If they do not interact: nothing happens

Features of the Axelrod model

- the dynamics tends to make interacting individuals more similar
- Interaction:
 - more likely for neighbors already sharing many traits (homophily)
 - becomes impossible when no trait is the same
- For each pair of neighbors: two stable configurations:
 - 1. when they are exactly equal, so that they belong to the same cultural region or
 - 2. when they are completely different, i.e., they sit at the border between cultural regions
- Starting from a disordered initial condition:
 - The evolution on any finite system leads to one of the many absorbing states, which belong to two classes:
 - 1. the **ordered states**, in which **all** individuals have the same set of variables, or
 - 2. Frozen states with different coexisting cultural regions (more numerous)
- Which one is reached: depends on q (number of possible traits):
 - Small q: quickly full consensus is achieved
 - Large q: very few individuals share traits → few interactions occur → formation of small cultural domains that are not able to grow (disordered frozen state)

Axelrod's model of cultural dissemination in a circle network (16 sec)

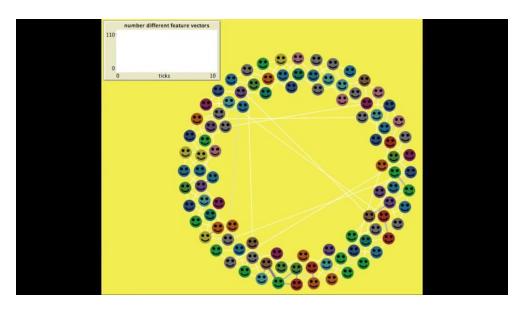


Inset: number of different feature vectors

- a circle interaction structure
- 100 agents, each
 - with 6 network contacts
 - 5 features
- Each feature can adopt 15 values
- Init: random set of traits
- Color of agents: one of the features
- Color and thickness of the lines: the overall similarity between the respective nodes
 - black thick lines: identical traits on all features
 - White thin lines: the two nodes are connected but maximally different.
- emergence of internally homogenous but mutually different clusters.
- Dynamics settled after 34,809 iterations with 19 cultural clusters.

(Michael Maes, 2015)

Axelrod's model of cultural dissemination in a small world network (47 sec)

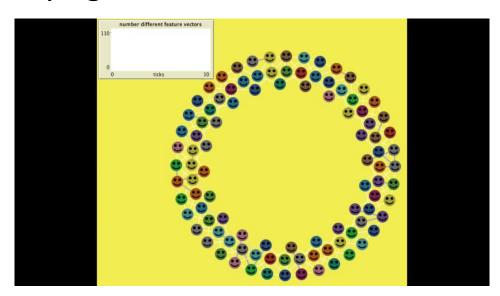


- a small-world interaction structure
- 100 agents, each
 - with 6 network contacts
 - 5 features
- Each feature can adopt 15 values
- Init: random set of traits
- Color of agents: one of the features
- Color and thickness of the lines: the overall similarity between the respective nodes
- emergence of internally homogenous but mutually maximally different clusters.
- Dynamics settled after 140,427 iterations with 7 cultural clusters.

Inset: number of different feature vectors

(Michael Maes, 2015)

Playing with Axelrod's model: the effect of globalization (53 sec)



Illustrates two implications of the model:

- 1. due to the rewiring the number of clusters in equilibrium decreased from 22 to 16
- 2. after the simulation continued (after rewiring) the number of unique combinations of cultural traits (diversity) first increased and then decreased
- (i) globalization decreases cultural diversity
- (ii) the short-term effects differ from the long-term effects

- Globalization: more individuals are in contact with others who are geographically very distant
- Circle NW interaction structure (at the beginning!)
- 100 agents, each
 - with 6 network contacts
 - 5 features
- Each feature can adopt 15 values
- Init: random set of traits
- Color of agents: one of the features
- Color and thickness of the lines: the overall similarity between the respective nodes
- The dynamics reaches a rest point (after 51,065 iterations)
- Rewire 20 links and cont. (modeling that individuals have more contact to distant others)

(Michael Maes, 2015)

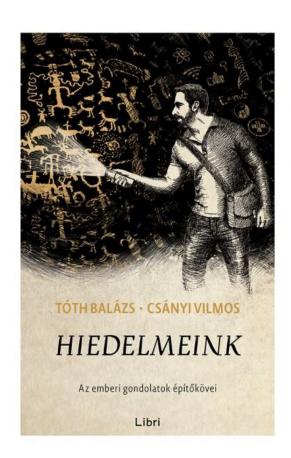
https://www.youtube.com/watch?v=VvXjk8P4TX0

37

The human belief system

A lot of knowledge has accumulated

- Neurobiology
- Various human sciences
- Psychology
- Anthropology
- Economics
- Political science
- Etc...



Fundamental Features of Human Belief Systems - What we do know

"Belief" (or "element of a BS"): all sorts of human thoughts — simple or complex — that can be transmitted with the use of language.

Beliefs...

- Form an interconnected system (no belief can exist in isolation)
- Not equally important
- Two belief/concept can be
 - Consistent, if they support each (Pathogens causes diseases" vs. "Contagion is due to the spread of pathogens")
 - Contradictory "Pathogens causes diseases" vs. "Evil spirits cause diseases"
- Seeks to be consistent: people try to maintain a belief system in which the elements mutually support each other, or are independent
 - If not: cognitive dissonance (CD) one of the most influential and well-researched theories in social psychology.
 - Strategies to keep them mutually supportive: "biases"
 - Accepting those which support the already existing ones
 - · Keeping touch with people from whom we expect similar opinions
 - Accepting beliefs that re-interpret the ones creating CD in a way that the CD dissolves (fake news)
 - Re-evaluating beliefs
- (Compartmentalized)

Most **models** assuming interrelated beliefs are coming from the political science.

Graph representation:

- A modular ("compartmentalized") hierarchical network
- Nodes: beliefs (attitudes, concepts, etc.)
- If they are related: edge between them
- Main principle: coherence/consistency maximization

Not a new idea.: Philip E. Converse: The nature of belief systems in mass publics (1964)

Further articles:

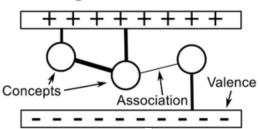
- DellaPosta, D. Pluralistic Collapse: The "Oil Spill" Model of Mass Opinion Polarization. Am. Sociol. Rev. 2020, 85, 507–536
- Turner-Zwinkels, F.M.; Johnson, B.B.; Sibley, C.G.; Brandt, M.J. Conservatives' Moral Foundations Are More Densely Connected Than Liberals' Moral Foundations. Personal. Soc. Psychol. Bull. 2020, 47, 167–184
- Brandt, M.J.; Sleegers, W.W.A. Evaluating Belief System Networks as a Theory of Political Belief System Dynamics. Personal. Soc. Psychol. Rev. 2021, 25, 159–185
- Baldassarri, D.; Goldberg, A. Neither Ideologues nor Agnostics: Alternative Voters' Belief System in an Age of Partisan Politics. Am. J. Sociol. 2014, 120, 45–95. [Google Scholar] [CrossRef]
- Brandt, M.J.; Sibley, C.G.; Osborne, D. What Is Central to Political Belief System Networks?
 Personal. Soc. Psychol. Bull. 2019, 45, 1352–1364.

Two crucial aspects of belief dynamics

Cognitive bias (or belief bias):

- <u>Def</u>: A person's tendency to accept arguments that supports a conclusion that aligns with his/her values, beliefs and prior knowledge, while rejecting counter arguments to the conclusion
- Leads to individual belief rigidity
- Cognitive dissonance (well-studied area)

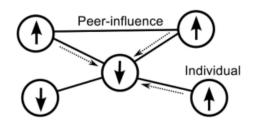
Cognitive Factors



Social influence:

- The tendency of individuals to become more similar when they interact (we have seen it at the Axelrod model)
- Leads to social conformity

Social Factors

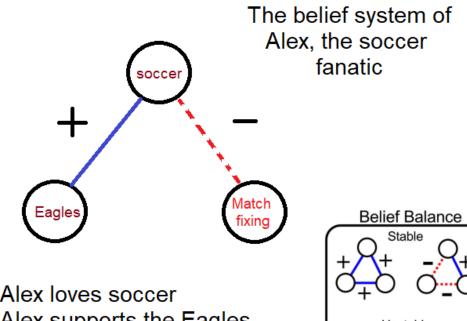


A cognitive-social model

- Individuals are embedded into a social NW, and social influence takes place via the social ties
- Each individual possesses a *network* of concepts and beliefs

The internal (in)coherence of each individual's belief network

is evaluated



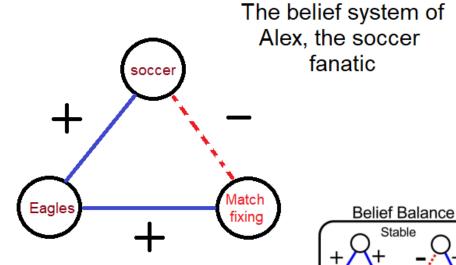
- 1) Alex loves soccer
- 2) Alex supports the Eagles

A cognitive-social model

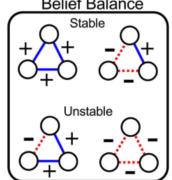
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- Each individual possesses a network of concepts and beliefs

The internal (in)coherence of each individual's belief network

is evaluated



- 1) Alex loves soccer
- 2) Alex supports the Eagles
- The eagles has been with match fixing



A cognitive-social model

 The internal coherence of each individual's belief network is evaluated by the internal energy function (on the belief NW M):

(For simplicity, the belief NW is complete, meaning that all concepts have a positive or negative association with every other)

$$E_n^{(i)} = -\frac{1}{\binom{M}{3}} \sum_{j,k,l} a_{jk} a_{kl} a_{jl}$$

 The evolution of belief systems is also driven by social interactions: social energy term, capturing the degree of alignment between connected individuals.)

 k_{max} is a normalization factor, maximum degree of N.

$$E_n^{(s)} = -rac{1}{k_{max}igg(rac{M}{2}igg)} \sum_{q \in \Gamma(n)} ec{S}_n \cdot ec{S}_q$$

S: belief state vector: each element corresponds to an edge

Total energy:

where

I: peer-influence ,

J: coherentism

$$H = \sum_{n \in \mathcal{N}} \left[JE_n^{(i)} + IE_n^{(s)} \right]$$

- The status of the entire society is characterized by
 - (i) the average internal coherence of the individuals $\langle E^{(i)} \rangle$, and
 - (ii) the homogeneity of the society $\langle E^{(s)} \rangle$

The simulation:

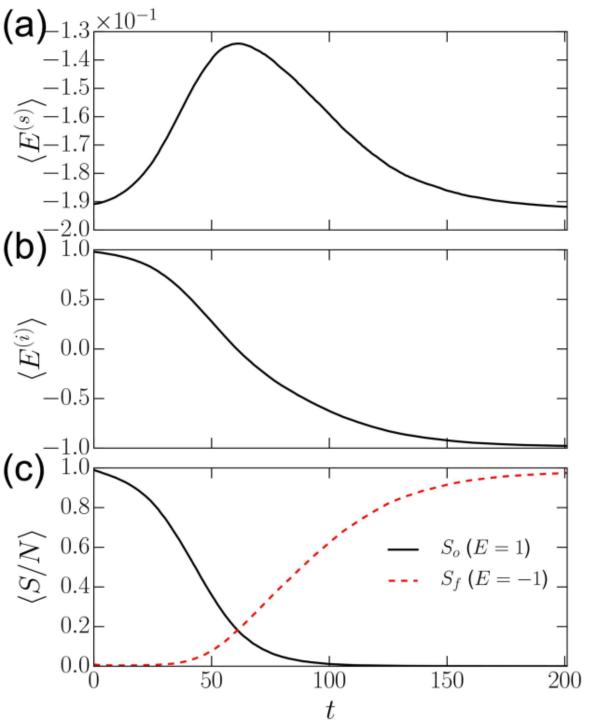
- At each time step a random pair of individuals is chosen
- One of the individuals (sender)randomly chooses a belief (association) from its internal belief system and sends it to the other individual (receiver)
- Assumption: each individual has an identical set of concept nodes
- The receiver accepts it if it decreases its individual energy H_n
- If $\Delta H_n > 0$, the receiver accepts it with probability $e^{-\Delta H_n}$
- T is "susceptibility" / "open-mindedness"

Results

- Given a homogeneous population of people with highly coherent belief systems, society remains stable.
- Given a homogeneous population of incoherent belief systems, society will become unstable and following a small perturbation, breaks down

In simulation:

- The society is initialized at consensus with an incoherent belief system.
- Then 1% of the population are given a random belief system
- Individuals attempt to reduce the energy of their own belief systems and leave consensus



In the simulation, the society is initialized at consensus with an incoherent belief system. Then 1% of the population are given a random belief system.

Strong societal consensus does not guarantee a stable society in our model. If major paradigm shifts occur and make individual belief systems incoherent, then society may become unstable.

- (a) The plot shows the evolution of social energy $E^{(s)}$ over time. The system starts at consensus but with incoherent beliefs. After introducing a small perturbation, individuals leave consensus, searching for more coherent sets of beliefs, until society reconverges at a stable configuration.
- **(b)** Decreasing mean individual energies $\langle E_{(i)} \rangle$ over time illustrates individual stabilization during societal transition.
- (c) $\langle S/N \rangle$ is the fractional group size. As society is upset, the original dominant but incoherent belief system S_o (solid black) is replaced by an emerging coherent alternative S_f (dashed red).